Thermochemistry of the Initial Steps of Methylaluminoxane Formation. Aluminoxanes and Cycloaluminoxanes by Methane Elimination from Dimethylaluminum Hydroxide and Its Dimeric Aggregates

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ABSTRACT: Results are presented of ab initio studies at levels MP2(full)/6-31G* and MP2(full)/6-311G** of the hydrolysis of trimethylaluminum (TMA, 1) to dimethylaluminum hydroxide (DMAH, 2) and of the intramolecular 1,2-elimination of CH4 from 2 itself to form methylaluminoxane (3), from its dimeric aggregate 4 to form hydroxytrimethylaluminoxane 5 and dimethylcyclodialuminoxane 6, and from its TMA aggregate 7 to form 8 and/or 9, the cyclic and open isomers of tetramethyldialuminoxane, respectively. Each methane elimination creates one new Lewis acid site, and dimethyl ether is used as a model oxygen-donor molecule to assess the most important effects of product stabilization by Lewis donor coordination. It is found that the irreversible formation of aggregate 4 (ΔG298 = −29.2 kcal/mol) is about three times more exergonic than the reversible formation of aggregate 7 (ΔG298 = −9.9 kcal/mol), that the reaction free enthalpies for the formations of 5 (ΔG298 = −9.0 kcal/mol) and 6 (ΔG298 = −18.8 kcal/mol) both are predicted to be quite clearly exergonic, and that there is a significant thermodynamic preference (ΔG298 = −7.2 kcal/mol) for the formation of 6 over ring-opening of 5 to hydroxytrimethylaluminoxane 10. The mechanism for oligomerization is discussed based on the bonding properties of dimeric aggregates and involves the homologation of HO-free aluminoxane with DMAH (i.e., 9 to 13), and any initially formed hydroxydialuminoxane 10 is easily capped to trialuminoxane 13. Our studies are consistent with and provide support for Sinn’s proposal for the formation of oligoaluminoxanes, and in addition, the results point to the crucial role played by the kinetic stability of 5 and the possibility to form cyclodialuminoxane 6. Dialuminoxanes 9 and 10 are reversed-polarity heterocumulenes, and intramolecular O-Al dative bonding competes successfully with Al complexation by Lewis donors. Intramolecular O-Al dative bonding is impeded in cyclodialuminoxane 6, and the dicoordinate oxygen in 6 is a strong Lewis donor. Ethylene polymerization catalysts contain highly oxophilic transition metals, and our studies suggest that these transition metal catalysts should discriminate strongly in favor of cycloaluminoxane-O donors even if these are present only in small concentrations in the methylaluminoxane (MAO) cocatalyst.

INTRODUCTION

The low-pressure polymerization of α-olefins with catalysts that combined aluminum alkyls and transition metal complexes (i.e., Ti, Zr) was discovered more than half a century ago, and the significance of the Ziegler–Natta polymerization has steadily increased ever since. The direct synthesis of triethylaluminum played a critical role for the initial success; trimethylaluminum has since become available commercially, and methyaluminoxane (MAO) is most usually employed as cocatalyst. A major advancement in transition metal catalysts occurred in the 1990s with reports by the groups of Brookhart and Gibson that described first examples of a new generation of homogeneous catalysts for ethylene polymerization. The precatalysts are neutral Fe(II) and Co(II) complexes formed by addition of tridentate pyridine bismine ligands to the appropriate metal salt. The precatalysts are employed in nonpolar organic solvents (toluene, isobutane) in the presence of a very large excess (100–1000 equiv) of MAO as cocatalyst. The iron catalysts showed better activities in both studies, and their performance parameters were comparable to the most active Ziegler–Natta catalysts. More recently, Sun and co-workers explored structurally similar bidentate bis(imino)pyridyl Fe(II) complexes, and tridentate 2,8-bis(imino)quinoline Fe(II) complexes, and related systems with nickel and titanium also have been studied.

While the organometallic precatalysts are well characterized, very little is known about the structure(s) and the function(s) of the active MAO species. Methylaluminoxane (MAO) is a generic term used to describe the products of “controlled” hydrolysis of trimethylaluminum (TMA, Me3Al), and modified methylaluminoxane...
(MMAO) is obtained by hydrolysis of TMA with admixtures of other trialkylaluminum compounds (e.g., tBu3Al). The compositions of MAO and MMAO are unknown, and they depend on their formation processes. In the BASF process, for example, MAO is prepared by addition of TMA to a slurry of CaSO4·1/2H2O in toluene.16 In patents by Ethyl Corporation, the synthesis of MAO is described by reaction of TMA with the hydrate of an alkali or alkaline earth metal hydroxide or halide, and the TMA/MX-hydrate ratio may vary between 2 and 1/2.17 In his recent review,4 Severn wrote that “apart from residual TMA, no other structural components or specific molecules have been unambiguously isolated and identified”. Still, one can begin with reasonable assumptions as to the types of reactions which occur during hydrolysis of TMA. There is no doubt that hydrolysis of alkyl—Al bonds will result in the formation of HO—Al bonds, the release of alkanes, and the formation of acyclic and cyclic systems with Al—O—Al bridges by further inter- and intramolecular alkane elimination, and the experimental studies of aluminoxanes by Barron,18–20 Pasynkiewicz,21 and Sinn22 suggest a plethora of chain, ladder, and cage structures (Scheme 1). Theoretical studies by Ziegler et al.,23 by Hall and co-workers,24 and by Linnolahti et al.,25 explored possible species with ladder and cage structures derived from dimethyldialuminum hydroxide (DMAH).

In his seminal 1995 paper,21 Sinn explored the structure of MAO formed from TMA on the surface of water ice at −40 °C, and the experimental results are consistent with a [Al4O3(Me)6]4+ cage cluster originally proposed by Barron.18 The experiments showed that the cluster may contain a molecule of TMA or solvent (ether, 1,4-dioxane, THF), and the dominant species in toluene and ether solution are [Al2O3(Me)6]8+(TMA)x (x = 0—4) and [Al2O3(Me)6]14+(OEt)2, respectively. Sinn convincingly argued for a cage structure formed by aggregation of four Al4O3Me8 trimers (Scheme 1). The proposals by Hall22 and by Linnolahti25 for potential MAO species bypass the Al4O3Me6 trimer. Hall discussed DMAH aggregates (Me2Al(OH))n (n = 2, 3, ...) and showed how the higher aggregates can lead to ladder-like structures by trans-annular CH4 elimination and that cage-like structures (MeAlO)n may result by reaction between the termini of ladder-type species. Linnolahti considered the coupling of cyclic oligomers (Me2Al(OH))n to nanotubular structures with concomitant CH4 elimination with dodecamer Al16O12Me24 as the thermodynamic sink. Hall and Linnolahti invoke intermolecular CH4 elimination to grow the aggregates, and Hall also invokes intramolecular 1,n-elimination (n = 4, 5, ...) to close cage structures.

We present here the results of ab initio studies of intramolecular 1,2-elimination of CH4 from dimethylaluminumhydroxide (DMAH, 2) itself to form methylaluminumoxide 3, from its dimeric aggregate 4 to form 5 and/or 6, and from its TMA aggregate 7 to form 8 and/or 9 (Scheme 2). Sinn discussed O(AlMe2)14 as “the monomer” following polyether nomenclature.26 We also employ the nomenclature for heterogeneous hydrides27 and refer to Me2Al—O—AlMe2 as permethylaluminumoxane, and 8 and 9 are its cyclic and open isomers, respectively. In analogy, the hydroxymethylaluminumoxane 10 is the acyclic isomer of 5. Aluminoxanes contain strong Lewis acidic and Lewis basic sites, and it is likely that their formations, their structures, and their functions are affected by aggregation and solvation. We are considering the smallest possible cyclic aggregates of DMAH, 4 and 7, because entropy favors these aggregates over larger cyclic aggregates. Each CH4 elimination creates one new Lewis acid site, and the elimination product thus may be stabilized by aggregation with an available Lewis donor.28 Aluminum is highly oxophilic,19 and product stabilization can be provided by other aluminoxanes and/or by donor molecules (i.e., water, ether),30 and/or anions (i.e., halides, sulfates, etc.) present during MAO formation. In the present study, dimethylether serves as a simple donor molecule to assess the most important product stabilization effects by Lewis donor coordination (Scheme 3). While the results of our studies are most directly applicable to ether solutions of aluminoxanes, we will emphasize throughout this article that we employ dimethylether as a simple donor molecule and that the discussion is therefore relevant for reaction systems that do not contain ethers but other O-donor molecules. At the beginning, we considered the study of the hydrates in the hope that we could learn about the intermediates of MAO formation and about donor-stabilized MAO species at the same time. We abandoned that approach because the hydrate complexes feature H2O···Al dative bonding and also hydrogen-bonding between water and O-sites in the MAO species. The focus of the present paper is on the comparison of the thermodynamic stabilities of...
different MAO species (rather than about the details of the reactions that connect the various MAO species), and for this purpose OMe 2 is a suitable donor to model donor-stabilized MAO species.

**COMPUTATIONAL METHODS**

Computations were performed with Gaussian03" on the 64-processor SGI Altix system of the UM Research Computing facilities. Potential energy surface (PES) analyses" were performed with second-order Møller–Plesset perturbation theory (MP2)" with all electrons included in the active space and in conjunction with the 6-31G* and 6-311G** basis sets." Vibrational analyses were carried out analytically for each stationary structure at the level of optimization to compute vibrational frequencies and molecular thermal energies, enthalpies, and entropies. Molecular models of stationary structures are shown in the figures, and Cartesian coordinates of all optimized structures are provided as Supporting Information. Total energies $E_{\text{tot}}$, vibrational zero-point energies (VZPE), thermal energies (TE), molecular entropies ($S$), and dipole moments ($\mu$) are documented in the Supporting Information as well. Isomer preference energies, activation, and reaction energies are discussed, and in Table 1 we report relative energies $\Delta E$, enthalpies, $\Delta H_298 = \Delta(E + \text{VZPE})$, and $\Delta H_298 = \Delta(E + \text{TE})$, and free enthalpies $\Delta G = \Delta(E + \text{TE} - 298.15 \cdot S)$.

All structures were computed at the MP2(full)/6-31G* level, and we discuss the results obtained at this level. The quality of this theoretical level is well established, and its economy allows for the computations of larger MAO systems. Nevertheless, we realize that the use of larger basis sets improves the Hartree–Fock wave functions especially of polar and strained molecules and that the increased virtual space provides for a better accounting of changes in electron correlation that accompany reactions. To assess basis set effects on the intrinsic reactions energies, 1–10 were computed again at the MP2(full)/6-311G** level. Using all pairs of reaction energies computed at the levels MP2(full)/6-31G* (Method 1) and MP2(full)/6-311G** (Method 2)," linear correlation results in the equations $\Delta H_298(M2) = 1.025 \cdot \Delta H_298(M1) + 5.890$ ($R^2 = 0.993$) and $\Delta G_298(M2) = 1.014 \cdot \Delta H_298(M1) + 5.534$ ($R^2 = 0.981$). For reactions that involve ether donor coordination, the values reported in Table 1 were determined by combining the respective value computed for the donor-free reaction at the MP2(full)/6-31G** level with the donor-coordination effect computed at the MP2(full)/6-31G* level.
### Table 1. Computed Relative and Reaction Energies (kcal/mol)

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<td>3 - OMe₂ + OMe₂ → 3 - (OMe₂)₂</td>
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**TMA Hydrolysis**

**TMA Aggregation**

**Methane 1,2-Elimination in Cycloadducts**

**Cycloadduct Formation**

**Ring-Opening of Cycloadduct 5**  

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<td>49</td>
<td>10 · (OMe₂)₂ → 6 · (OMe₂)₂ + CH₄</td>
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<td>–11.62</td>
<td>–18.02</td>
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Isodesmic Reaction

2 + Me–Al=O → 1 + HO–Al=O

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RESULTS AND DISCUSSION

Methane Elimination from DMAH. The reaction of water with trimethylaluminum (TMA, 1) affords dimethylaluminumhydroxide (DMAH, 2), and subsequent intramolecular CH₄ elimination from DMAH formally presents a path to the formation of methyaluminoxane 3. The computed structures of 1–3 and of their etherates are shown in Figure 1. The data computed for 1 · (OMe₂) agree very well with the measured ether binding energy (Hₑ = 21.92 ± 0.18 kcal/mol) and with the gas phase structure37 of 1 · (OMe₂). McMahon et al. reported the crystal structure of a related R₃Al(R’OH) complex, (Bu₃)₅Al [O(H)CH₂CH₂CH₂NMe₂].38

The reaction energies computed for reactions 1 + H₂O → 2 + CH₄ (eq 1) and 1 · OMe₂ + H₂O → 2 · OMe₂ + CH₄ (eq 9) are similar because of the comparable ether coordination energies of 1 and 2 (eqs 4 and 5), and the reactions are both highly exothermic and exergonic with reaction enthalpies and free reaction enthalpies of ΔH₂⁹⁸ < –40 and ΔG₂⁹⁸ < –40 kcal/mol. The elimination reaction 2 → 3 + CH₄ (eq 2) naturally is endothermic and endergonic, and the pertinent question is whether the energy released in the reaction 1 + H₂O → 2 + CH₄ (eq 1) might suffice to make 3 accessible via the overall reaction 1 + H₂O → 3 + 2 CH₄ (eq 3). The assessment of the effects of donor stabilization is more difficult in this case because methyaluminoxane 3 allows for primary Lewis donor coordination by two ether molecules (eqs 6–8). The first ether donor coordination of 3 is exergonic by ΔG₂⁹⁸ = –14.3 kcal/mol, and it is more than 6 kcal/mol higher in magnitude than the ether donor coordination free enthalpies of ΔG₂⁹⁸ ≈ –8 kcal/mol of 1 and 2. Note that most of this increase in free enthalpy is due to entropy effects. The second donor coordination of 3 is ΔG₂⁹⁸ ≈ –8.5 kcal/mol and not much different from the ether donor coordination of 1 and 2. The combined consequence (ca. 14.5 kcal/mol) of the stronger first donor coordination and of the additional second donor coordination reduces the endothermicity and the exergonicity of the reaction 2 · OMe₂ + OMe₂ → 3 · (OMe₂)₂ + CH₄ (eq 10) to ΔH₂⁹⁸ = 16.0 kcal/mol and ΔG₂⁹⁸ ≈ 19.9 kcal/mol, respectively.

Our computations therefore suggest, and this result might not be intuitive, that the formation of 3 from 1 via the reaction 1 · OMe₂ + HO + OMe₂ → 3 · (OMe₂)₂ + 2 CH₄ (eq 11) is significantly exothermic and exergonic by ΔH₂⁹⁸ = –28.2 kcal/mol and ΔG₂⁹⁸ ≈ –22.0 kcal/mol, respectively. While the formation of 2 is thermodynamically clearly favored over the formation of 3, the important point here is the recognition that the formation of the latter cannot be ignored based on the (false) assumption that 3 might not be accessible thermodynamically.

Self-Aggregation of TMA. We used 1 and 1 · OMe₂ as references in the computation of the reaction energies of hydrolysis in the absence or presence of donor molecules (eqs 1 and 9), and these are the proper references because self-aggregation of TMA is insignificant. Almenningen et al. recognized that the equilibrium 2 TMA ↔ (TMA)₂ is highly T-dependent in the gas phase (“trimethylaluminium gas at 60 °C and 30 mmHg consists of more than 97% dimers, while gas at 215 °C and the same pressure consists of more than 96% monomer”) and were able to determine the structures of TMA and of its dimer in the gas phase.39 The structures of TMA dimer and of trimeric aggregates (TMA)₂ · OMe₂ were considered to make this point (Figure 2).

It is true that the structure of the cyclic TMA dimer is greatly stabilized by dative bonding (ΔH₂⁹⁸ ≈ –20 kcal/mol, in excellent agreement with previous studies40); however, the
aggregation comes with an almost equally large entropy loss, and the formation of the cyclic TMA dimer is essentially thermoneutral (eq 12). The acyclic TMA dimer is a local minimum and about 8 kcal/mol less stable (eq 13). The cyclic dimer may form an aggregate with dimethylether as a very shallow minimum (eq 14), but this aggregate quickly collapses to the donor-coordinated acyclic TMA structure (eq 15). The formation of the sandwich structure seemed appealing because it allows for aggregates with any significant lifetime.

**Methane Elimination in the DMAH Dimer: Path to Cyclocyclodialuminoxane 6**? Instead of intramolecular CH₄ elimination to form 3, DMAH might self-aggregate in 4, and 2-fold CH₄ elimination may then lead to 5 and 6. Molecule 5 is the cycloadduct of DMAH and 3, and permethylcyclodialuminoxane 6 is the cycldimer of 3. The computed structures of 4—6 and of their etherates are shown in Figure 3.

The cyclic dimer (iBu₂AlOH)₂ was characterized spectroscopically, and the crystal structure was reported of the cyclic trimer (iBu₂AlOH)₃. Rogers et al. synthesized a large number of alkoxides [Me₂Al(OR)]ₙ and found that the compounds either are purely dimeric in solution or that both dimers and trimers occur. The most likely path for the formation of the trimer involves the addition of a monomer to a dimer, and the aggregation energy for the formation of 4 suggests that the conversion of the dimer to the trimer requires significant activation energy. Hence, the dimer should at least present a kinetic intermediate.

Structure 4 is C₂-symmetric, and the OH groups are placed in symmetrically bridging positions with d(O—Al) = 1.895 Å and about 10% longer than the bond length d(O—Al) = 1.729 Å in 2. The hydroxyl H-atoms are out of the Al₂O₂ plane with angle (O—O—H) = 139.8°. The ring angle at oxygen (Al—O—Al) = 98.4° is larger than the one at Al. Structure 6 is de facto C₂-symmetric, and all O—Al bond lengths are essentially the same, d(O—Al) = 1.768 Å and about 8% longer than the respective bond length of 1.630 Å in 3. The ring angle at oxygen (Al—O—Al) = 86.6° is smaller than the one at Al. Structure 5 is trapez-shaped; its base lengths are 1.697 and 2.051 Å; and its sides are 1.795 and 1.815 Å long. The “MeAlO” moiety in 5 is more 3-like than in 6, whereas the “Me₂AlOH” moiety in 5 is less 1-like than in 4. The ring angles in 5 are (Al—O—H) — (Al—O—Al) = 85.7° and (Al—O—Al) = 98.7°; the directions of the deviations from 90° angles are opposite to 4 and 6, and the hydroxyl group lies in the Al₂O₂ plane. All of these structural observations inform and are consistent with the discussion of bonding (vide infra).

We optimized the structures of etherates 5·(OMe₂) and 6·(OMe₂)₂ and considered both the cis and trans structures of the latter (Figure 3). As with ether adducts of 1—3, it is a common feature of these ether adducts that the ether—Al coordination is “wagged” i.e., the solvated Al atom does not lie in the best plane of the ether molecule. This feature appears on the MP2(full)/6-31G* potential energy surface, while it is absent in RHF-level computations. Whenever possible, the wagging of the ether plane occurs in such a way as to approach one or both of the ether-methyls more closely to an Al-bound oxygen; see 2·(OMe₂) in Figure 1 and 5·(OMe₂) and trans 6·(OMe₂)₂
in Figure 3. This intramolecular dispersion effect also is reflected in reduced $\angle (O-\text{Al} \cdot \cdot \cdot O_{\text{ether}})$ angles; see 2·(OMe$_2$) in Figure 1 in particular. The donor coordination enthalpies of of 5 and 6 (eqs 21 and 23) per ether donor are more than twice as large as for 2 and also exceed the complexation energy of 3.

The first methane elimination reaction $4 \rightarrow 5 + \text{CH}_4$ (eq 17) is endothermic by $\Delta H_{298} = 13.2$ kcal/mol, and it is only very slightly endergonic by $\Delta G_{298} = 2.5$ kcal/mol. The second methane elimination reaction $5 \rightarrow 6 + \text{CH}_4$ (eq 18) is almost thermoneutral with $\Delta H_{298} = -0.6$ kcal/mol, and it is quite clearly exergonic by $\Delta G_{298} = -11.0$ kcal/mol. Hence, the overall reaction $4 \rightarrow 6 + 2$ CH$_4$ (eq 19) remains somewhat endothermic by $\Delta H_{298} = 12.5$ kcal/mol, but it is clearly exergonic by $\Delta G_{298} = -8.5$ kcal/mol. Primary donor coordination always favors elimination, and reactions 27–29 all are clearly exothermic and exergonic. For the reaction $4 + 2$ OMe$_2 \rightarrow 6 \cdot$ (OMe$_2$)$_2 + 2$ CH$_4$ (eq 29), we computed $\Delta H_{298} = -41.4$ kcal/mol and $\Delta G_{298} = -36.3$ kcal/mol.

**Methane Elimination in TMA-Complexed DMAH: Dialuminoxane 9.** DMAH can aggregate with TMA, which is available in large excess, and intramolecular CH$_4$ elimination might lead to tetramethyldialuminoxane as either the cyclic isomer 8 or the open isomer 9. The computed structures of 7 and 9 and of their etherates are shown in Figures 4 and 5. Searches of the potential energy surfaces in regions with the geometries of 8 and 8·(OMe$_2$) led to the respective open isomer. A methyl bridge is obviously too weak to make up for the strain it would cause in 8. This finding suggests that the methyl bridge in 7 also should be rather weak. When presented with the opportunity to replace the additional dative bond by the methyl bridge by a Lewis donor molecule, the Me$_2$Al moiety is expected to opt for the latter, and hence, we considered the structure of the monoetherate 7·(OMe$_2$).

As with 4, cycloadduct 7 has a symmetry plane that includes the OH group; the hydroxyl group is bridging symmetrically with $d(O-\text{Al}) = 1.884$ Å; the hydroxyl-H is out of the plane of the four-membered ring with $\angle (\text{C} \cdot \cdot \cdot \text{O}-\text{H}) = 140.6^\circ$; and the ring angle at oxygen $\angle (\text{Al}-\text{O}(\text{H})-\text{Al}) = 93.2^\circ$ is greater than 90°. The bond lengths of the methyl bridge are $d(C-\text{Al}) = 2.147$ Å, about 10% longer than the exocyclic Al–Me bonds (1.961 Å), and the kite-shaped ring features a ring angle at
carbon of $\angle (\text{Al-Me-Al}) = 79.2^\circ$. It is not surprising that the methyl bridge of 7 is easily broken by an ether donor to form $7\cdot(\text{OMe}_2)$, but the thermochemistry of the addition of the Lewis donor to 7 is quite interesting (eq 24). To begin with, the
donor coordination free enthalpy $\Delta G_{298}(7)$ is almost twice as large as $\Delta G_{298}(2)$! Structure $7 \cdot (\text{OMe}_2)$ is TMA-complexed $2 \cdot (\text{OMe}_2)$, and this Lewis acid complexation should increase the Lewis acidity of $2$. One would expect stronger complexation of $7$ than of $2$ for enthalpy reasons. Yet, the ether donor binding energy is much lower for $7$ compared to $2$ ($\Delta H_{298}(7) > \Delta H_{298}(2)$), and in spite of this lower enthalpy, the donor complexation free enthalpy of $7$ is much more endergonic than for $2$ ($\Delta G_{298}(7) < \Delta G_{298}(2)$). Therefore, the reaction $7 + \text{OMe}_2 \rightarrow 7 \cdot (\text{OMe}_2)$ presents a case of entropy-driven binding enhancement caused by the Lewis acid (TMA) complexation. To rationalize this situation, one can argue that the free enthalpy of complexation of $2$ by TMA includes a premium because the restriction of internal motions due to the methyl bridging reduces the molecular entropy of the Lewis acid adduct $7$. The ether donor coordination of $7$ lifts this restriction, and the dative bond formation thus releases energy previously stored in reduced molecular entropy.

Structure $9$ is a reversed-polarity heterocumulene, and this recognition explains the linearity at the central O atom (Scheme 4). The nonpolar canonical structure of the parent allene and its usual heteroanalogues (i.e., CO$_2$) contains two cumulated double bonds between a divalent four-electron center and two six-electron termini (i.e., A-I, CO$_2$-I); the important polar resonance forms II–IV shift electron density to the termini; and reversed-polarity resonance forms V–VII play no role. In contrast, cumulene resonance form I is highly polar in the case of $9$, and the reversed-polarity resonance forms V–VII shift electron density to the center and reduce the molecular polarity. The nonpolar structure $9$–VII dominates; the O $\rightarrow$ Al $\pi$-dative bond formations remain partial; and the Al atoms remain the centers of Lewis acidity.

The structure of the pyridine-coordinated tert-butyl analogue of $9$ has been reported, and its Al$_3$O moiety is linear in the crystal. It is an interesting structural feature of $9 \cdot (\text{OMe}_2)$ and $9 \cdot (\text{OMe}_2)_2$ that their bond angles at oxygen remain rather high with 144.7$^\circ$ and 144.3$^\circ$, respectively. The structures of $9 \cdot (\text{OMe}_2)_n$ also show that ether donor coordination does not cause complete pyramidalization at the Al centers. The strength of the first ether donor coordination in $9$ is $\Delta H_{298} = -22.6$ kcal/mol and very close to the ether binding energy $\Delta H_{298} = -22.8$ kcal/mol of $2$, and entropy makes the donor binding of $9$ slightly better (eqs 25 and 26).

The methane elimination reaction $7 \rightarrow 9 + \text{CH}_4$ (eq 20) is exothermic by $\Delta H_{298} = -8.6$ kcal/mol and exergonic by $\Delta G_{298} = -23.6$ kcal/mol. Primary ether donor complexation favors the elimination product $9$, and we computed $\Delta H_{298} = -37.3$ kcal/mol and $\Delta G_{298} = -37.5$ kcal/mol for reaction $7 \cdot (\text{OMe}_2) + \text{OMe}_2 \rightarrow 9 \cdot (\text{OMe}_2)_2 + \text{CH}_4$ (eq 33).

The free enthalpy of the single CH$_4$ elimination $7 \rightarrow 9 + \text{CH}_4$ (eq 20) is about 26 kcal/mol more exergonic than the single CH$_4$ elimination $4 \rightarrow 5 + \text{CH}_4$ (eq 12), and it is still about 15 kcal/mol
more exergonic than the double methane elimination \( \text{eq 19} \). This ordering persists in the presence of a strong Lewis donor, but there are two major differences: First, the free reaction enthalpies of reactions 29 and 33 are almost the same. Second, reaction 27 remains about 22 kcal/mol less exergonic compared to reaction 33, but reaction 27 definitely becomes exergonic under these conditions. We thus conclude that product donor stabilization opens the reaction channel leading to 5 and cyclodialuminoxane 6.

Aggregation Energies and Competition between Cycloadducts 4 and 7. The geometries of 4 – 7 and 9 inform about the bonding of the four-membered rings and their stability toward ring opening and/or fragmentation. The main resonance forms of 4 – 8 are shown in Scheme 5. The bonding in 4 and 7 is best described by hybrids of the degenerate pair of resonance forms I and II. Structure 5 shows structural features indicative of 5-I (short bond length of trapez base) and 5-II (long bond length of trapez base), and the placement of the OH group in the \( \text{Al}_2\text{O}_2 \) plane reflects the dominance of 5-II (as in derivatives of MeAl(OH)\(_2\)). Resonance forms 6-I and 6-II contribute equally, and 6-III dominates the bonding of 6. The bonding of structures in the PES region in the proximity 8 is dominated by 8-II, and the dative bond is too weak to ensure structural integrity. We know that 5 is a minimum on the potential energy surface and that the dative bond involving the HO donor must be stronger than the dative bond in 7 involving the methyl bridge. Nevertheless, 5-II indicates that ring opening is an option for 5, and breaking of the weakest, dative Al\( \cdots \)O bond would lead to acyclic 10. We discuss the significance of this reaction channel below.

There is no question that the products of CH\(_4\) elimination from 4 are much more stable with respect to fragmentation than 4. The fragmentation reactions 5 \( \rightarrow \) 2 + 3 (eq 35) and 6 \( \rightarrow \) 2 3 (eq 36) are endergonic by 76.0 and 121.8 kcal/mol, respectively, and the analogous reactions of the ether-coordinated species (eqs 39 and 40) also are endergonic by 63.3 and 103.9 kcal/mol, respectively. Clearly, these fragmentations of 5 and 6 cannot occur under the conditions of typical MAO formation reactions.

There also is no doubt that DMAH would rather dimerize to 4 than form the mixed aggregate 7 with TMA. We find that the dimerization is preferred by about 20 kcal/mol in the absence (eqs 34 and 37) or presence of a Lewis donor (eqs 38 and 42). Moreover, the aggregation energies show that dimer 4 is essentially stable toward fragmentation, whereas the formation of 7 is reversible.

The ratio 4/7 therefore should depend on the relative concentrations of 2 and 1, and the ratio may increase over time. If the hydrolysis of TMA is conducted in such a way as to keep the local concentration of 2 low relative to 1, then one would expect the formation of aggregate 7 and consequently the production of Sinn monomer 9 by CH\(_4\) elimination. In a TMA hydrolysis process that allowed for a higher relative concentration of 2, one would expect the formation of dimer 4 and consequently the irreversible production of 5 by methane elimination.

Ring Opening of Cycloadduct 5 to Hydroxytrimethyldialuminoxane 10. We computed the structures of hydroxytrimethyldialuminoxane 10, of the monoetherate \( \text{OMe}_3 \) formed by unimolecular ring opening of 5 \( \cdot \) (\( \text{OMe}_2 \)), and of the
dietherate 10·(OMe₂), and molecular models of these structures are shown in Figure 6.

The ring-opening reaction 5 → 10 is essentially thermoneutral (eq 43), and hence, Lewis donors can affect this reaction in an interesting fashion. The unimolecular ring opening of 5·(OMe₂) initially leads to 10·(OMe₂), and subsequent Lewis donor addition then results in 10·(OMe₂)₂. Alternatively, a Lewis donor might assist in the bimolecular ring-opening process Me₂O + 5·(OMe₂) → 10·(OMe₂)₂. The reaction energy of the unimolecular reaction 5·(OMe₂) → 10·(OMe₂) is essentially determined by the difference of the donor binding energies of 5 and 10 (eqs 21 and 44), and this reaction is endergonic (eq 46) by ΔG₂⁹⁸ = 5.8 kcal/mol. On the other hand, the second donor binding of 10 causes the bimolecular reaction 5·(OMe₂) + OMe₂ → 10·(OMe₂)₂ to become clearly exergonic with ΔG₂⁹⁸ = −8.5 kcal/mol (eq 47). Hence, intermediate 5 may have some lifetime if the bimolecular reaction is slowed by low temperature and/or scarcity of the Lewis donor and the formation of cyclodialuminoxane 6 becomes possible. On the other hand, in an abundance of Lewis donor one must expect the fast, quantitative, and essentially irreversible ring opening of 5 to 10.

Assessment of Basis Set Effects on Reaction Equilibria.

To assess basis set effects on the intrinsic reaction energies, compounds 1—10 were computed again at the MP2(full)/6-311G** level. The hydrolysis reaction 1 and the methane elimination reactions 2, 3, and 17—20 are predicted to be significantly harder (less exothermic, more endothermic) at the better theoretical level, whereas the reaction energies for association reactions 34—37 and the ring-opening reaction 43 are less sensitive to theoretical level effects. These effects echo in the reaction energies that include donor complexation and provide additional support for the four key findings:

1. The reaction free enthalpies for the formations of aggregates 4 and 7 (eqs 38 and 42) are quite similar at levels M1 and M2, and aggregate 4 (ΔG₂⁹⁸(38) = −29.2 kcal/mol) is about three times more stable than aggregate 7 (ΔG₂⁹⁸(42) = −9.9 kcal/mol).

2. The reaction free enthalpies for the formations of 5 and 6 (eqs 27 and 29) are markedly less exergonic at the M2 level (ΔG₂⁹⁸(27) = −9.0 and ΔG₂⁹⁸(29) = −18.8 kcal/mol), whereas the respective value for the formation of 9 is affected much less (ΔG₂⁹⁸(30) = −33.1 kcal/mol). The result that matters for the chemistry is the finding that both reactions 27 and 29 are predicted to be quite clearly exergonic at the better level.

3. The unimolecular and the donor-assisted bimolecular ring-opening reactions of 5 to 10 (eqs 46 and 47) remain endergonic and exergonic, respectively, and the reaction free enthalpies are ΔG₂⁹⁸(46) = 3.2 kcal/mol and ΔG₂⁹⁸(47) = −11.1 kcal/mol at the better level.

4. The thermodynamic preference for the formation of 6 over ring opening to 10 (eq 49) is significantly reduced; however, the preference persists, and reaction 49 remains strongly exergonic (ΔG₂⁹⁸(49) = −7.2 kcal/mol).

From Dialuminoxane to Tri- and Tetraaluminoxane. We have argued that tetramethyldialuminoxane 9 and hydroxytri- methylaluminoxane 10 are the main products of CH₄ elimination from aggregate 7 and dimer 4, respectively, and that the ratio [4]/[7] depends on the relative concentrations of 2 and 1. We now consider how the results of our study inform mechanistic discussions of aluminoxane oligomerization.
The reaction of water with an aluminum species involves precoordination of water to the aluminum species and subsequent CH₄ elimination. Since self-aggregating of TMA is at best weak, it is most probable that water reacts with a free TMA molecule rather than with a TMA molecule of 7. Nonaggregated DMAH is extremely scarce, and hence, a second hydrolysis of DMAH is much less probable than hydrolysis of TMA. The computed aggregation energies further suggest a low probability for direct hydroxylation 9 + H₂O → 10 + CH₄ because any structure with an Al–O bond is capable of forming stable aggregates.

We briefly return to Scheme 5 to clarify the options for CH₄ elimination from the cycloadducts. Aside from single covalent bonds, there are two dative bonds in both resonance forms I and II of both 4 and 7; there are two dative bonds and one double bond in resonance forms I of 5 and 8; while form II contains only one dative bond; and the resonance forms of 6 feature either two dative bonds and two double bonds or only single bonds. Structures of types 4, 5, and 6 can thus be distinguished by the minimal number of dative bonds (MNDB) that occur in their resonance forms, and the values are MNDB(4) = 2, MNDB(5) = 1, and MNDB(6) = 0. For an MNDB = 1 structure, the resonance form with just one dative bond indicates the oppure site location for facile ring opening. A resonance form with two dative bonds reflects on possible formations and/or fragmentations of the cycloadduct, and fragmentations are likely only if MNDB = 2. In a chain growth reaction with CH₄ elimination, the substrate will be formed by aggregation of two moieties with two dative bonds; the product of CH₄ elimination will have at least one dative bond (MNDB = 1), and the location of that dative bond will indicate the position of the ring opening to afford the chain-elongated acyclic product.

Formally, one can consider any specific CH₄ elimination to occur “across a covalent bond” (i.e., 4-I → 5-I, 5-I → 6-I, 7-I → 8-I) or “across a dative bond” (4-II → 5-II, 5-II → 6-III, 7-II → 8-II), and the result always is a reduction of MNDB by 1. The latter perspective is convenient because formal elimination across dative bonds directly leads to the MNDB = 1 resonance form of the product. The latter perspective also is physically more appropriate since the structural features suggest that resonance forms with Al=O bonds are minor contributors. The isodesmic reaction 2 + Me–Al=O → 1 + HO–Al=O is endothermic by more than 10 kcal/mol (Table 1), and hence, the contributions of resonance forms with a RO–Al=O moiety should be markedly reduced compared to the contribution of resonance forms that contain a Me–Al=O moiety.

Suppose the initial phase of TMA hydrolysis has occurred, all water has been captured in DMAH and its aggregates, and 9 has not been formed (Scheme 6). The aggregation of 9 with DMAH to form 11 (eq 50) is more exothermic than the aggregation of TMA with DMAH in 7 (eq 37). The equilibrium 9 + 7 = 11 + 1 (eq 52) is therefore exothermic, and aggregate 11 (Figure 7) becomes accessible at least in low concentration. The CH₄ elimination 11 → 12 + CH₄ (eq 53) is analogous to reaction 4 → 5 + CH₄ (eq 17), and one would expect that donor stabilization of the elimination product 12 would be necessary to render the elimination exothermic as with the reaction 4 + OMe₂ → 5 (OMe₂) + CH₄ (eq 27). Interestingly, our results show that the CH₄ elimination 11 → 12 + CH₄ (eq 53) is exothermic even without donor-stabilization of the product. As can be seen in Figure 7, structure 12 benefits from intramolecular dative bonding between one methyl group of the in-ring AlMe₂ moiety and the exocyclic AlMe₂ group. An interaction of this kind prior to the CH₄ elimination is precluded because the approach of the exocyclic AlMe₂ group to the methyl of one in-ring AlMe₂ moiety is sterically impeded by the other in-ring AlMe₂ moiety in 11. The ring opening of 12 trialuminoxane 13 (eq 54) is formally similar to the ring opening of 5 to 10 (eq 43); the free reaction enthalpies of both reactions are less than 1 kcal/mol; and donor stabilization favors the open structures. As with 9, 13 is a reversed-polarity heterocumulene with essentially linear Al–O–Al units. The OAl₉ bonds (1.710 Å) are slightly shorter than the OAl₈ bonds (1.717 Å) and the OAl bonds (1.718 Å) in 9.

If one considers the reaction 9 + 2 → 13 formally as a CH₄ elimination across a dative bond of 11-I, one obtains 12-I, the MNDB = 1 resonance form of 12, and cleavage of the dative bond in 12-I leads to product 13a with the DMAH’s OAl₂Me₂ moiety (shown in green) added to the end of the chain. If one considers the CH₄ elimination across the dative bond of 11-II, then one obtains 12-Ib, and ring opening leads to 13b: the product of insertion of the DMAH’s OAl₂Me₂ moiety into an Al–O bond of 9. The two endocyclic AlMe₂ groups in 11 are chemically equivalent, and there is no reason to assume that the exocyclic AlMe₂ moiety would be able to prefer one over the other; hence, the chain elongation proceeds essentially in equal parts by addition (13a) and by insertion (13b).

Now, suppose that some 10 has been formed in the initial phase of TMA hydrolysis. With the availability of 10, a variety of reaction channels become viable because 10 may aggregate with any one of its three Al–O bonds, and there may be regiochemical options for CH₄ elimination from the resulting aggregates. Hydroxyaluminoxane 10 can form a 7-analogue aggregate 14 with TMA, and CH₄ elimination can lead to the formation of trialuminoxane 13 (Scheme 7).

The optimized structure of adduct 14 is shown in Figure 7. One is fully justified to consider 14 as an alternative adduct of DMAH of 9; while the Al–OH bond of 2 coordinates to one of the Al–O bonds of 9 to form 11, the Al–OH bond of 2 would coordinate an Al–Me bond to form isomer 14. However, the thermochemical data of eqs 57– 59 show that 14 is not accessible by addition of DMAH to 9. The formation of 14 by aggregation of 10 and TMA is possible thermodynamically (eqs 60 and 61), and moreover, the equilibrium 10 + 1 = 14 is driven to the right by the high TMA concentrations and by the removal of 14 by the highly exothermic methane elimination and trialuminoxane formation (eq 62). All attempts to find minima of types 15 and 16 on the potential energy surface inadvertently lead to 13. Structures 8 and 15 are topologically similar, and one would expect the additional O-substituent to further reduce the aluminum’s Lewis acidity.

This type of reaction (i.e., 2 → 9, 10 → 13) should dominate for any compound with an Al–OH bond in an abundance of TMA. Elimination of methane across the dative bond in 14-I eliminates one of TMA’s methyl groups and leads via 15-type structures to 13a, whereas elimination of CH₃ across the dative bond in 14-II eliminates one of the methyl groups of 9 and leads via 16-type structures to 13c, formally the product of TMA addition to Me₃Al–O–Al=O. Cycloadduct 14 is asymmetric; one expects a regiochemical preference; and formation of 13a should be preferred because contributions by 15-II (Me–Al=O) are more important than contributions by 16-I (RO–Al=O).

The minimal mechanism for the growth of oligoaluminoxanes thus involves the homologation of HO-free aluminoxane with...
tetraaluminoxane can be formed in analogy. Hence, our studies for the formation of oligoaluminoxanes.

**CONCLUSION**

If the hydrolysis of TMA is conducted in such a way as to keep the local concentration of 2 low relative to 1 (slow addition of water to TMA solution, vigorous stirring, low temperature, etc.), then one would expect the formation of TMA-DMAH aggregate and consequently the production of Sinn monomer 9 by CH4 elimination. Homologation via 7-analogue 9-DMAH aggregates affords trialuminoxanes 13, and higher aluminoxanes are then accessible in analogy.

In a process for TMA hydrolysis that would allow for a higher relative concentration of 2 (fast addition of water to TMA solution, etc.; slow addition of TMA solution to water, etc.), one would expect the formation of the rather stable DMAH dimer and consequently the production of 5 by CH4 elimination. The simplest outcome would occur under reaction conditions that favor the ring opening of 5 to 10 and the subsequent capping of 10 with TMA to form 13. Since the homologation of 9 provides the same outcome, the path via 10 cannot be excluded.

Our structural studies suggest that the formation of cyclodialuminoxane 6 is thermodynamically possible under reaction conditions that (a) provide product stabilization to 6 and that (b) grant 5 some lifetime. There is an apparent dilemma here in that Lewis donors facilitate the ring opening of 5, but we believe that this challenge can be addressed. In the presence of a sterically demanding donor, for example, it should be possible to slow the bimolecular ring opening of 5 without lowering the product stabilization of 6. We have employed dimethylether merely as a simple model of a donor molecule, and the important donors in MAO chemistry (halides, sulfates, etc. used in MAO production; oxygen in aluminoxanes, ...) remain to be identified.

Dialuminoxanes 9 and 10 are reversed-polarity hetero cumulenes, and O → Al dative bonding reduces the Lewis donor ability of the central oxygen in acyclic aluminoxanes toward Lewis acids. The bond angle at oxygen remains above 140° in 9 ·(OMe2)2 and 10 ·(OMe2)2 that is, intramolecular dative binding in 9 and 10 competes successfully with Al-complexation by the ether donors! In cyclodialuminoxane 6, on the other hand, intramolecular O → Al dative bonding is impeded, and the dicordinate oxygen in 6 is a strong Lewis donor. The Lewis donor strength at oxygen is significantly different for acyclic and cyclic dialuminoxanes, and this difference in their electronic structures has important consequences for the chemistry in the presence of Lewis acids with high oxophilicity. Oxophilic Lewis acids may provide additional product stabilization to cyclodialuminoxanes in the course of MAO formation. Alkali metal ions are known for their high oxophilicity, 16 and alkali metal salts are added in some processes for MAO formation. More importantly, the ethylene polymerization catalysts all contain highly oxophilic transition metals, 15 and our studies suggest that these transition metal catalysts should discriminate strongly in favor of cycloaluminoxane-O donors even if these are present only in small concentrations in the MAO cocatalyst.

**ASSOCIATED CONTENT**

Supporting Information. Tables of total energies and thermochemical data computed at MP2(full)/6-31G* and MP2-(full)/6-311G** and Cartesian coordinates of stationary structures. This material is available free of charge via the Internet at http://pubs.acs.org.

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(35) For this comparison, the back reaction 43 was considered, i.e., the formation of 5 from 10.


